

```

g[x_] := x - (x^2 - 2) / (2 x);

p0 = 1.; (* Initial guess*)
tol = 10^-6;
Nmax = 20;
(* Make changes above this line *)
n = 0;
outList = {};
Print["Fixed Point Iteration for g(x) = ", g[x],
  " : initial guess p0 = ", p0, ", tol = ", N[tol], ", and Nmax = ", nMax];
While[n < Nmax,
  p1 = g[p0];
  If[Abs[p1 - p0] <= tol,
    Print["|p_{n+1} - p_n| <= tol, and best estimate is p", n, " = ", p1]; Break[]];
  Print["n = ", n, "\tp_{n+1} = ", p1, "\tp_{n+1} - p_n = ", p1 - p0];
  p0 = p1;
  n++;
];
If[n == nMax, Print["Fixed point Iteration did not converge to tolerance ",
  tol, " with Nmax = ", Nmax] ];

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Fixed Point Iteration for  $g(x) = x - \frac{-2 + x^2}{2x}$ 
  : initial guess p0 = 1., tol =  $1. \times 10^{-6}$ , and Nmax = 10
n = 0    p_{n+1} = 1.5    p_{n+1} - p_n = 0.5
n = 1    p_{n+1} = 1.41667    p_{n+1} - p_n = -0.0833333
n = 2    p_{n+1} = 1.41422    p_{n+1} - p_n = -0.00245098
n = 3    p_{n+1} = 1.41421    p_{n+1} - p_n =  $-2.1239 \times 10^{-6}$ 
|p_{n+1} - p_n| <= tol, and best estimate is p4 = 1.41421

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g[x_] := x - (x^2 - 2) / (2 x);
p0 = 3.; (* Initial guess*)
tol = 10^-6;
Nmax = 10;
(* Make changes above this line *)
n = 0;
outList = {};
Print["Fixed Point Iteration for g(x) = ", g[x],
  " : initial guess p0 = ", p0, ", tol = ", N[tol], ", and Nmax = ", nMax];
While[n < Nmax,
  p1 = g[p0];
  AppendTo[outList,
    {n, N[p1, 18], N[p1 - p0], N[p1 - p], N[Abs[p1 - p] / Abs[p0 - p]],
      N[Abs[p1 - p] / Abs[p0 - p]^phi], N[Abs[p1 - p] / Abs[p0 - p]^2]}];
  If[Abs[p1 - p0] <= tol, Print["|p_{n+1} - p_n} <= tol, and best estimate is p",
    n, " = ", p1]; Break[]];
  p0 = p1;
  n++];
If[n == nMax, Print["Fixed point Iteration did not converge to tolerance ",
  tol, " with Nmax = ", Nmax] ];
Print[TableForm[outList, TableHeadings -> {None,
  {"n", "p_{n+1}", "p_{n+1} - p_n", "p_{n+1} - p", "R(1,n)", "R(phi,n)", "R(2,n)"} }]];

```

Fixed Point Iteration for  $g(x) = x - \frac{-2 + x^2}{2x}$   
 : initial guess  $p_0 = 3.$ ,  $tol = 1. \times 10^{-6}$ , and  $Nmax = 10$

$|p_{n+1} - p_n| <= tol$ , and best estimate is  $p_4 = 1.41421$

n	p_{n+1}	p_{n+1} - p_n	p_{n+1} - p	R(1,n)	R(phi,n)	R(2,n)
0	1.83333	-1.16667	0.41912	0.264298	0.315196	0.166667
1	1.46212	-0.371212	0.0479076	0.114305	0.0819998	0.272727
2	1.415	-0.0471228	0.000784868	0.0163829	0.00513276	0.341969
3	1.41421	-0.00078465	$2.17674 \times 10^{-7}$	0.000277339	0.0000180688	0.353357
4	1.41421	$-2.17674 \times 10^{-7}$	$1.66533 \times 10^{-14}$	$7.65059 \times 10^{-8}$	$2.18255 \times 10^{-10}$	0.35147

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g[x_] := x - (x^2 - 2) / (2 x);
p = Sqrt[2]; (* the fixed point of g *)
p0 = 3.; (* Initial guess*)
tol = 0;
Nmax = 10;
(* Make changes above this line *)
phi = (Sqrt[5] - 1) / 2;
n = 0;
outList = {};
Print["Fixed Point Iteration for g(x) = ", g[x],
  " : initial guess p0 = ", p0, ", tol = ", N[tol], ", and Nmax = ", nMax];
While[n < Nmax,
  p1 = g[p0];
  AppendTo[outList,
    {n, N[p1, 18], N[p1 - p0], N[p1 - p], N[Abs[p1 - p] / Abs[p0 - p]],
      N[Abs[p1 - p] / Abs[p0 - p]^phi], N[Abs[p1 - p] / Abs[p0 - p]^2]}];
  If[Abs[p1 - p] <= tol, Print["|p_{n+1} - p_n} <= tol, and best estimate is p",
    n, " = ", p1]; Break[]];
  p0 = p1;
  n++;
If[n == nMax, Print["Fixed point Iteration did not converge to tolerance ",
  tol, " with Nmax = ", Nmax]];
Print[TableForm[outList, TableHeadings -> {None,
  {"n", "p_{n+1}", "p_{n+1} - p_n", "p_{n+1} - p", "R(1,n)", "R(phi,n)", "R(2,n)"}]}];

```

Fixed Point Iteration for  $g(x) = x - \frac{-2 + x^2}{2x}$

: initial guess  $p_0 = 3.$ ,  $tol = 0.$ , and  $Nmax = 10$

$|p_{n+1} - p_n| <= tol$ , and best estimate is  $p_6 = 1.41421$

n	p_{n+1}	p_{n+1} - p_n	p_{n+1} - p	R(1,n)	R(phi,n)	R(2,n)
0	1.83333	-1.16667	0.41912	0.264298	0.315196	0.16666
1	1.46212	-0.371212	0.0479076	0.114305	0.0819998	0.27272
2	1.415	-0.0471228	0.000784868	0.0163829	0.00513276	0.34196
3	1.41421	-0.00078465	$2.17674 \times 10^{-7}$	0.000277339	0.0000180688	0.35335
4	1.41421	$-2.17674 \times 10^{-7}$	$1.66533 \times 10^{-14}$	$7.65059 \times 10^{-8}$	$2.18255 \times 10^{-10}$	0.35147
5	1.41421	$-1.68754 \times 10^{-14}$	$-2.22045 \times 10^{-16}$	0.0133333	$7.27814 \times 10^{-8}$	8.0064
6	1.41421	$2.22045 \times 10^{-16}$	0.	0.	0.	0.