

The Way Dr. Swift thinks about Cubic Bézier Curves

A Bézier curve in the plane \mathbb{R}^2 is

$$\{ \vec{r}(t) \mid 0 \leq t \leq 1 \}$$

where $\vec{r}(t) = \vec{a} + \vec{b}t + \vec{c}t^2 + \vec{d}t^3$.

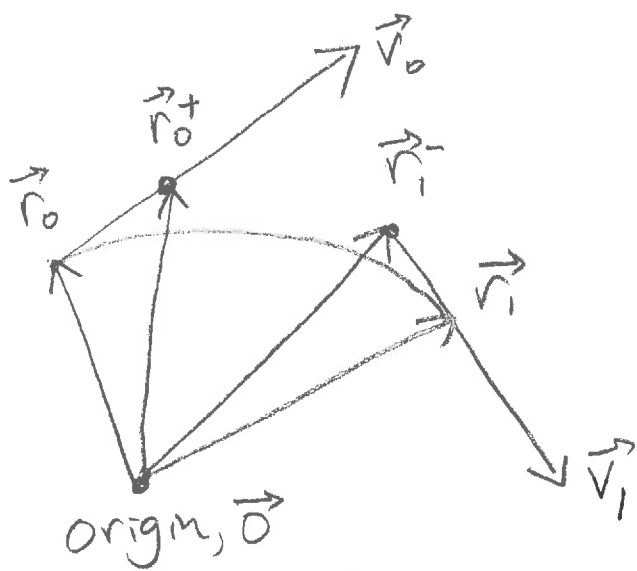
The vector constants \vec{a} , \vec{b} , \vec{c} and \vec{d} are chosen to satisfy given data $\vec{r}_0, \vec{r}_1, \vec{v}_0, \vec{v}_1$, where the velocity vectors are given "in code" based on guide points \vec{r}_0^+ and \vec{r}_1^- .

$$\vec{r}(0) = \vec{r}_0$$

$$\vec{r}(1) = \vec{r}_1$$

$$\vec{r}'(0) = \vec{v}_0 = 3(\vec{r}_0^+ - \vec{r}_0)$$

$$\vec{r}'(1) = \vec{v}_1 = 3(\vec{r}_1^- - \vec{r}_1)$$



The constants are

$$\vec{a} = \vec{r}_0$$

$$\vec{b} = \vec{v}_0$$

in terms of
Position & Velocity

$$\vec{c} = 3(\vec{r}_1 - \vec{r}_0) - \vec{v}_1 - 2\vec{v}_0$$

$$\vec{d} = -2(\vec{r}_1 - \vec{r}_0) + \vec{v}_1 + \vec{v}_0$$

or, in terms of guide points:

$$\vec{a} = \vec{r}_0$$

$$\vec{b} = 3(\vec{r}_0^+ - \vec{r}_0)$$

$$\vec{c} = 3(\vec{r}_0 + \vec{r}_1^- - 2\vec{r}_0^+)$$

$$\vec{d} = \vec{r}_1 - \vec{r}_0 + 3\vec{r}_0^+ - 3\vec{r}_1^-$$